

# Package ‘ttTensor’

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**Type** Package

**Title** Tensor-Train Decomposition

**Version** 1.0.2

**Date** 2025-08-25

**Suggests** testthat

**Depends** R (>= 3.5.0)

**Imports** methods, rTensor, PTak, Matrix

**Description** Tensor-train is a compact representation for higher-order tensors. Some algorithms for performing tensor-train decomposition are available such as TT-SVD, TT-WOPT, and TT-Cross. For the details of the algorithms, see I. V. Oseledets (2011) <[doi:10.1137/090752286](https://doi.org/10.1137/090752286)>, Yuan Long, et al (2017) <[doi:10.48550/arXiv.1709.02641](https://doi.org/10.48550/arXiv.1709.02641)>, I. V. Oseledets (2010) <[doi:10.1016/j.jaa.2009.07.024](https://doi.org/10.1016/j.jaa.2009.07.024)>.

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**URL** <https://github.com/rikenbit/ttTensor>

**NeedsCompilation** no

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ttTensor-package	<i>Tensor-Train Decomposition</i>
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## Description

Tensor-train is a compact representation for higher-order tensors. Some algorithms for performing tensor-train decomposition are available such as TT-SVD, TT-WOPT, and TT-Cross. For the details of the algorithms, see I. V. Oseledets (2011) <doi:10.1137/090752286>, Yuan Longao, et al (2017) <doi:10.48550/arXiv.1709.02641>, I. V. Oseledets (2010) <doi:10.1016/j.laa.2009.07.024>.

## Details

The DESCRIPTION file:

```

Package:      ttTensor
Type:         Package
Title:        Tensor-Train Decomposition
Version:      1.0.2
Date:         2025-08-25
Authors@R:   c(person("Koki", "Tsuyuzaki", role = c("aut", "cre"), email = "k.t.the-answer@hotmail.co.jp"), person("Manabu", "Ishii", role = c("aut", "cre"), email = "m.ishii@rikenbit.jp"))
Suggests:    testthat
Depends:      R (>= 3.5.0)
Imports:      methods, rTensor, PTAK, Matrix
Description:  Tensor-train is a compact representation for higher-order tensors. Some algorithms for performing tensor-train decomposition are available such as TT-SVD, TT-WOPT, and TT-Cross.
License:      MIT + file LICENSE
URL:         https://github.com/rikenbit/ttTensor
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Maintainer:  Koki Tsuyuzaki <k.t.the-answer@hotmail.co.jp>

```

Index of help topics:

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TTCross	Tensor-Train Decomposition by TRCross
TTSVD	Tensor-Train Decomposition by TTSVD
ttTensor-package	Tensor-Train Decomposition
TTWOPT	Tensor-Train Decomposition by Tensor-train
	Weighted OPTimization
unfold	Unfold a Tensor

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**References**

I. V. Oseledets, (2011). Tensor-Train Decomposition. *SIAM J. SCI. COMPUT.*  
Yuan, Longhao, et. al., (2017). Completion of high order tensor data with missing entries via tensor-train decomposition. *International Conference on Neural Information Processing*  
I. V. Oseledets, et. al., (2010). TT-cross approximation for multidimensional arrays. *Linear Algebra and its Applications*  
Ali Civril, et. al., (2009). On selecting a maximum volume sub-matrix of a matrix and related problems. *Theoretical Computer Science*

**See Also**

[TTSVD](#), [TTWOPT](#), [TTCross](#), [skeleton.decomp](#), [maxvol](#)

**Examples**

```
ls("package: ttTensor")
```

---

as\_sptensor

*Convert to Simple Sparse Tensor*

---

**Description**

Converts an array or matrix to a simple sparse tensor format. This is a minimal implementation to replace the tensorr dependency.

**Usage**

```
as_sptensor(x)
```

**Arguments**

x                    An array or matrix to convert

**Details**

This function provides a minimal sparse tensor implementation to support the TTCross function without requiring the archived tensorr package. For production use with actual sparse data, consider using specialized sparse tensor packages.

**Value**

A simple\_sparse\_tensor object

## Examples

```
# Create a 3D array
x <- array(rnorm(24), dim = c(2, 3, 4))

# Convert to sparse tensor format
sparse_x <- as_sptensor(x)
```

---

dtensor

*Dense Tensor Creation*

---

## Description

Creates a dense tensor representation. This is a compatibility function that simply returns the input as-is.

## Usage

```
dtensor(x)
```

## Arguments

x                    An array or matrix

## Details

This function is provided for compatibility with code that previously used the `tenorr` package. It simply returns the input without modification.

## Value

The input array or matrix unchanged

## Examples

```
# Create a 3D array
x <- array(rnorm(24), dim = c(2, 3, 4))

# Create dense tensor (returns x unchanged)
dense_x <- dtensor(x)
```

---

maxvol	<i>maxvol algorithm</i>
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### Description

maxvol finds the  $r \times r$  submatrix of maximal volume in  $C$  ( $n \times r$ ) by greedily searching the vector of max norm, and subtraction of its projection from the rest of rows. See also [http://tensorly.org/stable/\\_modules/tensorly/cont](http://tensorly.org/stable/_modules/tensorly/cont)

### Usage

```
maxvol(C)
```

### Arguments

`C` The input sparse matrix.

### Value

`row_idx` : The indices of rows, which make the determinant as large

### Author(s)

Koki Tsuyuzaki

### References

Ali Civril, et. al., (2009). On selecting a maximum volume sub-matrix of a matrix and related problems. *Theoretical Computer Science*

### See Also

[skeleton.decomp](#)

### Examples

```
library("Matrix")
# Matrix data
X3 <- matrix(runif(10*20), nrow=10)
X3 <- as(X3, "sparseMatrix")
# Skeleton Decomposition
out.SKD <- skeleton.decomp(X3, r=3, num.iter=2, thr=1E-5)
```

---

skeleton.decomp      *Skeleton Decomposition*

---

### Description

skeleton.decomp decomposes the input sparse matrix ( $n*m$ ) and return the three matrices  $C$  ( $n*r$ ),  $U$  ( $r*r$ ), and  $R$  ( $r*m$ ). Only sparse matrix defined by the Matrix package is acceptable as the input.

### Usage

```
skeleton.decomp(A, r, thr=1E-10, num.iter=30)
```

### Arguments

A	The input sparse matrix.
r	Rank parameter to specify the lower dimension ( $r \leq \min(A)$ ).
thr	The threshold to determine the convergence (Default: 1E-10).
num.iter	The number of iteration (Default: 30).

### Value

$C$  :  $A[I, :]$   $U$  :  $\text{inverse}(A[I, J])$   $R$  :  $A[:, J]$  rowidx : The indices of rows colidx : The indices of columns  
 RecError : The reconstruction error between data matrix and reconstructed matrix from  $C$ ,  $U$ , and  $R$   
 RelChange : The relative change of the error

### Author(s)

Koki Tsuyuzaki

### References

I. V. Oseledets, et. al., (2010). TT-cross approximation for multidimensional arrays. *Linear Algebra and its Applications*

### See Also

[maxvol](#)

### Examples

```
library("Matrix")
# Matrix data
X3 <- matrix(runif(10*20), nrow=10)
X3 <- as(X3, "sparseMatrix")
# Skeleton Decomposition
out.SKD <- skeleton.decomp(X3, r=3, num.iter=2, thr=1E-5)
```

**Description**

TTCross incrementally decomposes the input tensor by skeleton decomposition algorithm. The algorithm only select the row/column indices and any large temporal matrix are genrated in the process. Therefore, this method is suitable for the sparse tensor.

**Usage**

```
TTCross(A, Ranks=NULL, thr=1E-10, num.iter=30)
```

**Arguments**

A	The input sparse tensor.
Ranks	TT-ranks to specify the lower dimensions.
thr	The threshold to determine the convergence (Default: 1E-10).
num.iter	The number of iteration (Default: 30).

**Value**

G : Core tensors

**Author(s)**

Koki Tsuyuzaki

**References**

I. V. Oseledets, et. al., (2010). TT-cross approximation for multidimensional arrays. *Linear Algebra and its Applications*

**Examples**

```
# TTCross requires sparse tensor input
# Creating a simple example
library("rTensor")
X1 <- array(rnorm(3*4*5), c(3,4,5))
X1 <- as.tensor(X1)
# Convert to sparse format
X2 <- as_sptensor(dtensor(X1@data))
# TT-ranks (should be less than dimensions)
Ranks <- c(p=2, q=2)
# Note: TTCross is designed for sparse tensors
# and may have numerical issues with some inputs
tryCatch({
  out.TTCross <- TTCross(X2, Ranks, num.iter=2)
```

```

    print("TTCross completed")
  }, error = function(e) {
    print("TTCross encountered an error - this function is experimental")
  })
}

```

---

TTSVD

*Tensor-Train Decomposition by TTSVD*


---

### Description

TTSVD incrementally decomposes the input tensor by singular value decomposition (SVD).

### Usage

```
TTSVD(A, Ranks=NULL, accuracy=NULL)
```

### Arguments

A	The input tensor.
Ranks	TT-ranks to specify the lower dimensions.
accuracy	The accuracy of the compression.

### Value

G : Core tensors

### Author(s)

Koki Tsuyuzaki

### References

I. V. Oseledets, (2011). Tensor-Train Decomposition. *SIAM J. SCI. COMPUT.*

### Examples

```

library("rTensor")
# Tensor data
X1 <- array(rnorm(3*5*7*9*11), c(3,5,7,9,11))
dimnames(X1) <- list(
  I=paste0("i", 1:3),
  J=paste0("j", 1:5),
  K=paste0("k", 1:7),
  L=paste0("l", 1:9),
  M=paste0("m", 1:11)
)
X1 <- as.tensor(X1)
# TT-ranks

```

```
Ranks <- c(p=2, q=4, r=6, s=8)
# TTSVD
out.TTSVD <- TTSVD(X1, Ranks)
out.TTSVD <- TTSVD(X1, accuracy=1E-10)
```

TTWOPT

*Tensor-Train Decomposition by Tensor-train Weighted OPTimization***Description**

TTWOPT incrementally decomposes the input tensor by gradient descent. The tensor with missing entries is also specified with weight tensor W.

**Usage**

```
TTWOPT(X, Ranks, W=NULL, eta=1E-7, thr=1E-10, num.iter=100)
```

**Arguments**

X	The input tensor.
Ranks	TT-ranks to specify the lower dimensions.
W	The weight tensor to specify the missing entries (0: missing, 1: existing). The size must be same as that of X.
eta	The learning rate parameter of the gradient descent algorithm (Default : 1E-10).
thr	The threshold to determine the convergence (Default: 1E-10).
num.iter	The number of iteration (Default: 30).

**Value**

G : Core tensors  
 RelChange : The relative change of the error  
 f : The values of the object function  
 RecError : The reconstruction error between data tensor and reconstructed tensor from C, U, and R

**Author(s)**

Koki Tsuyuzaki

**References**

Yuan, Longhao, et. al., (2017). Completion of high order tensor data with missing entries via tensor-train decomposition. *International Conference on Neural Information Processing*

**Examples**

```

library("rTensor")
# Tensor data
X1 <- array(rnorm(3*5*7*9*11), c(3,5,7,9,11))
dimnames(X1) <- list(
  I=paste0("i", 1:3),
  J=paste0("j", 1:5),
  K=paste0("k", 1:7),
  L=paste0("l", 1:9),
  M=paste0("m", 1:11)
)
X1 <- as.tensor(X1)
# TT-ranks
Ranks <- c(p=2, q=4, r=6, s=8)
# TTWOPT
out.TTWOPT <- TTWOPT(X1, Ranks, eta=1E-7)

```

---

 unfold

*Unfold a Tensor*


---

**Description**

Unfolds a tensor along a specified mode into a matrix representation.

**Usage**

```
unfold(x, mode)
```

**Arguments**

x	A tensor object (simple_sparse_tensor, Tensor, array, or matrix)
mode	The mode along which to unfold the tensor

**Details**

This function unfolds a tensor along the specified mode into a matrix. It supports simple\_sparse\_tensor objects, rTensor Tensor objects, and regular arrays/matrices. The function uses rTensor's rs\_unfold internally.

**Value**

A matrix representation of the unfolded tensor

**Examples**

```
library(rTensor)

# Create a 3D tensor
x <- array(rnorm(24), dim = c(2, 3, 4))
tensor_x <- as.tensor(x)

# Unfold along mode 1 (using ttTensor's unfold function)
unfolded <- ttTensor::unfold(tensor_x, mode = 1)
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