

Package ‘episplineDensity’

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Title Density Estimation with Soft Information by Exponential
Epi-splines

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the Matlab code of Royset and Wets

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Depends nloptr, pracma

Description Produce one-dimensional density estimates using
exponential epi-splines. The user may incorporate soft information, by
imposing constraints that (i) require unimodality; (ii) require that the
density be monotone non-increase or non-decreasing; (iii) put upper bounds
on first or second moments; (iv) bound the density's values at mesh points;
(v) require that the estimate be continuous or continuously differentiable;
and more.

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R topics documented:

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 expepi

Fit density estimate by exponential epi-splines.

Description

This code produces one-dimensional density estimates satisfying "soft" conditions like unimodality. A number of possible soft conditions are permitted. This version calls the nloptr suite of optimizers. Convergence is not particularly fast.

Usage

```
expepi(data, lower = NULL, upper = NULL, N = 10, M = 5,
       order = 2, softinfo, opt.args, opt.local.args, postproc.controls)
```

Arguments

| | |
|-------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| data | Numeric vector of data for density estimate. |
| lower | Lower bound for density support. If missing, use default as set in preprocess.data |
| upper | Upper bound for density support. If missing, use default as set in preprocess.data |
| N | Integer: number of segments. Default 10. |
| M | Integer: number of points within each segment to consider. Default 5. |
| order | Integer: order of polynomials used in spline fits. Currently this must be 2. |
| softinfo | List of "soft" conditions to be imposed on the density estimate. See setup.softinfo for possibilities. |
| opt.args | List of arguments to be passed to global optimizer. See setup.optargs for defaults and more information. Set <code>print_level = 1</code> to show each iteration in the global optimizer, which might help convince you that something is happening. |
| opt.local.args | List of arguments to be passed to local optimizer. See setup.optargs for defaults and more information. |
| postproc.controls | List of arguments for post-processing. See postproc.control for defaults and more information. |

Details

This function produces a density estimator for data `data`, imposing constraints in `softinfo`. The density is in the form of an exponential epi-spline. An epi-spline is like a spline estimator in that it consists of polynomials between knots. However, the polynomials are not automatically constrained to meet at knots. The density estimate is an exponential epi-spline, which is $\exp(-s)$ where s is the epi-spline value.

Value

A list of class `c("episplineDensity", "nloptr")` with the output from `nloptr`, plus additional items:

| | |
|----------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>softinfo</code> | The <code>softinfo</code> as passed to the optimizer, consisting of what was passed into this function plus some defaults |
| <code>epiparameters</code> | Epiparameters, as generated by preprocess.data |
| <code>caseinfo</code> | A list with the sample size, as <code>sampleisize</code> , and <code>notion</code> else. |
| <code>x</code> | Copy of the data |
| <code>c.out</code> | Coefficients associated with this set of data. |
| <code>opts</code> | Copy of <code>opts</code> . See setup.optargs . |
| <code>orig.integral</code> | If the postprocessing option <code>normalize.to.1</code> is supplied, this item is present and gives the value of the integral of the density before normalization. It should be near 1. |
| <code>integral</code> | If the postprocessing option <code>normalize.to.1</code> is supplied, this item is present and gives the value of the integral of the density after normalization. It should exactly 1. |

Author(s)

Sam Buttrey, after Matlab code from Royset and Wets.

References

Royset and Wets, Nonparametric Density Estimation with Soft Information Using Exponential Epi-Splines, in press.

See Also

[nloptr](#)

Examples

```
##---- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,
##--or do help(data=index) for the standard data sets.

n10 <- c(-0.795173769, -0.268865287, -0.032803042, -0.361751212,
0.699170399, -0.909275685, 0.452956532, 1.501356616, 1.669061521,
-0.524919503)
#
# Generate a unimodal estimate. Plot automatically.
#
## Not run: soft <- setup.softinfo (10, unimodal = TRUE)

## Not run: expepi (n10, softinfo = soft)
#
# Generate a unimodal estimate, but constrain the second non-central
```

```

# moment to be <= 0.4. Plot automatically. This command will require
# a couple of minutes to run.
#
## Not run: soft$upperbound2moment <- 0.4
## Not run: expepi (n10, softinfo = soft)
#
# Generate a nondecreasing estimate without plotting.
#
## Not run: soft <- setup.softinfo (10, monotone="nondecreasing")
## Not run: n10.out <- expepi (n10, softinfo = soft, postproc.controls =
  postproc.control (pic.types = NULL))
## End(Not run)
#
# Now plot.
#
## Not run: plot (n10.out)

```

plot.episplineDensity *Plot an exponential epi-spline density estimate*

Description

Plot a density estimate, plus the original data

Usage

```

## S3 method for class 'episplineDensity'
plot(x, ...)

```

Arguments

| | |
|-----|------------------------------------|
| x | Output from a call to expepi |
| ... | Other arguments, currently ignored |

Details

This plots the x.pts and y.est items from the x object, and adds red circles for the original observations.

Value

None.

Author(s)

Sam Buttrey

See Also

[expepi](#)

postproc.control *Set options for post-processing of expepi output*

Description

Generate a list of options for post-processing expepi output.

Usage

```
postproc.control(numevalpts = 10000, pic.types = c("1"), normalize.to.1 = TRUE)
```

Arguments

| | |
|----------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| numevalpts | Integer, giving number of equally-spaced points at which to compute density estimate. Default 10,000. |
| pic.types | Character vector, naming the types of pictures produced. Default "1", which produces a graph of the density with points in red circles. |
| normalize.to.1 | The density should integrate to exactly 1, but sometimes the numeric value is a little different from 1. If this is TRUE, the density's values are scaled so that the integral is exactly 1. |

Value

A list of preprocessing options with the values of the arguments.

Note

Currently only one picture is supported.

Author(s)

Sam Buttrey

See Also

[expepi](#), [~~~](#)

`preprocess.data`*Preprocess data to construct epiparameters.*

Description

The epispline parameters are the data plus lower and upper bounds on the support of the estimated density.

Usage

```
preprocess.data(data, lower, upper)
```

Arguments

| | |
|--------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>data</code> | Numeric vector of data to be used in density estimation. |
| <code>lower</code> | Lower bound on density support. Default: if missing or NULL, the lower bound is taken to be $\min(x) - 2 * \text{sd}(x)$. If <code>-inf</code> , the lower bound is taken to be $\text{mean}(x) - 10 * \text{sd}(x)$. |
| <code>upper</code> | Upper bound on density support. Default: if missing or NULL, the upper bound is taken to be $\max(x) + 2 * \text{sd}(x)$. If <code>inf</code> , the upper bound is taken to be $\text{mean}(x) + 10 * \text{sd}(x)$. |

Details

Data outside the bounds is discarded.

Value

List of epiparameters, with entries

| | |
|-------------------|---------------------------------------------------------|
| <code>data</code> | Data as passed, with entries outside the bounds deleted |
| <code>m0</code> | Lower bound |
| <code>mN</code> | Upper bound |

Author(s)

Sam Buttrey, from matlab code by Royset and Wets

See Also

[expepi](#)

```
print.episplineDensity
```

Print method for episplineDensity objects.

Description

This prints the status item and nothing else.

Usage

```
## S3 method for class 'episplineDensity'  
print(x, ...)
```

Arguments

| | |
|-----|------------------------------------------------|
| x | Output from a call to expepi . |
| ... | Other arguments, currently ignored. |

Details

The current intent of this is to keep this whole object from printing to the screen.

Value

None

Author(s)

Sam Buttrey

See Also

[expepi](#)

```
setup.optargs
```

Set up arguments for global and local optimization programs

Description

The exponential epi-spline scheme uses a global optimization routine from package `nloptr` that itself calls a local one. This function produces a list of options for either or both.

Usage

```
setup.optargs(param.length, opts, local.opts)
```

Arguments

| | |
|--------------|---------------------------------------------------------------------------------------------------------------|
| param.length | Length of parameter vector. |
| opts | Options to global solver. These will be passed as argument "opts" to nloptr . |
| local.opts | Options to local solver. These will be passed as a list named "local_opts" attached to the "opts" list above. |

Details

Default values for opts are algorithm = "NLOPT_LD_AUGLAG", maxeval = 2500, xtol_rel = 1e-05, xtol_abs = 1e-05, and for local.opts, algorithm = "NLOPT_LD_SLSQP", maxeval = 1000, and xtol_rel = 1e-05.

Value

List with default opts overridden by any that were supplied, plus a list named local_opts with default local_opts, overridden by any that were supplied.

Author(s)

Sam Buttrey

See Also

[expepi](#)

| | |
|----------------|-----------------------------------------------------|
| setup.softinfo | <i>Set up softinfo for exponential epi-splines.</i> |
|----------------|-----------------------------------------------------|

Description

The softinfo prescribes constraints imposed on the density estimate.

Usage

```
setup.softinfo(N = 10, order = 2, warn = FALSE, ...)
```

Arguments

| | |
|-------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| N | Integer giving number of interior mesh points (knots) for the splines. Default 10. |
| order | Integer giving the order for the polynomial splines. Default 2, and only 2 is permitted right now. |
| warn | Logical: emit warnings when contradictory conditions are imposed? Currently ignored. It is easy to generate contradictory conditions and the code only tests for a few combinations. |

...

A set of named arguments describing the possible values of soft information. The current possibilities are:

M Numeric : number of points in each segment at which Fisher and other constraints are imposed

unimodal Logical: if TRUE, require that the density be unimodal.

unimodaluppertail, unimodalldowntail Numeric. Impose unimodality only on the lower or upper floor ($N * \text{unimodalldowntail}$) or floor ($N * \text{unimodaluppertail}$) segments.

monotone Character: describes what sort of monotonicity is required. Possible values "nondecreasing" or "nonincreasing".

lowerboundsk, upperboundsk Numeric, length $N+1$. Bounds on epiparameters $s[0]$ through $s[N]$. See [expepi](#) for details. Default: -1000 for lower, $+1000$ for upper.

lowerboundak0, upperboundak0, lowerboundakp, upperboundakp Numeric, length N . Lower and upper bounds on the linear coefficients ($ak0$) and quadratic coefficients (akp) of the splines.

continuous, continuousDiff, lsc, usc Logicals. When TRUE, require continuity, continuous differentiability, or that the density be lower semi-continuous (lsc) or upper semi-continuous (usc).

pointwiseFisherLower, pointwiseFisherUpper Numeric, length 1. Lower and upper bound on the value of slope/value at every point in every segment.

lowerdensityvalue, upperdensityvalue Numeric vectors of length N giving lower and upper bounds on the density estimate inside segments.

lowerdensityvalueEndpt, upperdensityvalueEndpt Numeric vectors of length $N + 1$ giving lower and upper bounds on the density estimate at segment end points.

lowerdensityvalueSpecific Two-column numeric matrix. Each row has an x value and a density value and the density estimate is constrained to be at least $\text{lowerdensityvalueSpecific}[j,2]$ at $x = \text{lowerdensityvalueSpecific}[j,1]$ for each row j .

KLDivergenceUpper, KLDivergenceLower, KLDensity, KLDensityParams Upper and lower bounds on the KL divergence of the density estimate from the density whose name is given as an R density function in **KLDensity**, e.g. `dnorm`, and whose parameters are given as a list in **KLDensityParams**, e.g. `list(mean = 0, sd = 1)`

upperbound1moment, upperbound2moment Numeric; upper bounds on the first or second (non-central) moment of the estimate

Value

List with any specified values, plus any defaults (notably $M = 5$).

Author(s)

Sam Buttrey, after Matlab code by Royset and Wets.

See Also

[expepi](#)

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