Package 'GenOrd'

May 16, 2013

Type Package

Title Simulation of ordinal and discrete variables with given correlation matrix and marginal distributions

Version 1.1.0

Date 2013-05-16

Author Alessandro Barbiero, Pier Alda Ferrari

Maintainer Alessandro Barbiero <alessandro.barbiero@unimi.it>

Description The package implements a procedure for generating samples from ordinal/discrete random variables with pre-specified correlation matrix and marginal distributions.

License GPL

LazyLoad yes

Depends mvtnorm, Matrix, MASS

R topics documented:

GenOrd-package 2
contord 3
corrcheck 4
ordcont 5
ordsample 6

Index **9**

GenOrd-package *Simulation of ordinal and discrete variables with given correlation matrix and marginal distributions*

Description

The package implements a procedure for generating samples from ordinal/discrete random variables with pre-specified correlation matrix and marginal distributions. It is developed in two steps: the first step (function `ordcont`) sets up the original continuous variables in order to achieve the final discrete/ordinal variables meeting the experimental conditions; the second step (`ordsample`) generates samples from the adjusted original variables and discretizes them, thus simulating samples from the target variables. The procedure can handle both Pearson's correlation and Spearman's rho, and any finite support for the discrete variables. The intermediate function `contord` computes the correlations of discrete/ordinal variables derived from correlated normal variables through discretization. Function `corrcheck` returns the lower and upper bounds of the correlation coefficients of ordinal/discrete variables given their marginal distributions, i.e. returns the range of feasible pairwise correlations. This version has fixed some inconsistencies regarding Spearman correlation coefficient that affected the two previous versions.

Details

Package:	GenOrd
Type:	Package
Version:	1.1.0
Date:	2012-05-16
License:	GPL
LazyLoad:	yes

Author(s)

Alessandro Barbiero, Pier Alda Ferrari Maintainer: Alessandro Barbiero <alessandro.barbiero@unimi.it>

References

P.A. Ferrari, A. Barbiero (2012) Simulating ordinal data, Multivariate Behavioral Research, 47(4), 566-589

See Also

`contord`, `ordcont`, `corrcheck`, `ordsample`

contord *Correlations of discretized variables*

Description

The function computes the correlation matrix of the k variables, with given marginal distributions, derived discretizing a k-variate standard normal variable with given correlation matrix

Usage

```
contord(marginal, Sigma, support = list(), Spearman = FALSE)
```

Arguments

marginal	a list of k elements, where k is the number of variables. The i-th element of marginal is the vector of the cumulative probabilities defining the marginal distribution of the i-th component of the multivariate variable. If the i-th component has k_i categories, the i-th element of marginal will contain $k_i - 1$ probabilities (the k_i-th is obviously 1).
Sigma	the correlation matrix of the standard multivariate normal variable
support	a list of k elements, where k is the number of variables. The i-th element of support contains the ordered values of the support of the i-th variable. By default, the support of the i-th variable is $1, 2, ..., k_i$
Spearman	if TRUE, the function finds Spearman's correlations (and it is not necessary to provide support), if FALSE (default) Pearson's correlations

Value

the correlation matrix of the discretized variables

Author(s)

Alessandro Barbiero, Pier Alda Ferrari

See Also

ordcont, ordsample, corrcheck

Examples

```
# consider 4 discrete variables
k<-4
# with these marginal distributions
marginal<-list(0.4,c(0.3,0.6),c(0.25,0.5,0.75),c(0.1,0.2,0.8,0.9))
# generated discretizing a multivariate standard normal variable
# with correlation matrix
Sigma<-matrix(0.6,4,4)
diag(Sigma)<-1
# the resulting correlation matrix for the discrete variables is
contord(marginal,Sigma)
# note all the correlations are smaller than the original 0.6
# change Sigma, adding a negative correlation
```

```
Sigma[1,2]<--0.2
Sigma[2,1]<-Sigma[1,2]
Sigma
contord(marginal, Sigma)
```

---

corrcheck *Checking correlations*

Description

The function returns the lower and upper bounds of the correlation coefficients of the ordinal/discrete variables given their marginal distributions, i.e. returns the range of feasible pairwise correlations.

Usage

```
corrcheck(marginal, support = list(), Spearman = FALSE)
```

Arguments

marginal	a list of k elements, where k is the number of variables. The i-th element of marginal is the vector of the cumulative probabilities defining the marginal distribution of the i-th component of the multivariate variable. If the i-th component has k_i categories, the i-th element of marginal will contain $k_i - 1$ probabilities (the k_i-th is obviously 1).
support	a list of k elements, where k is the number of variables. The i-th element of support contains the ordered values of the support of the i-th variable. By default, the support of the i-th variable is $1, 2, ..., k_i$
Spearman	TRUE if we consider Spearman's correlation, FALSE (default) if we consider Pearson's correlation

Value

The functions returns a list of two matrices: the former contains the lower bounds, the latter the upper bounds of the feasible correlations (on the extra-diagonal elements)

Author(s)

Alessandro Barbiero, Pier Alda Ferrari

See Also

contord, ordcont, ordsample

Examples

```
# four variables
k<-4
# with 2, 3, 4, and 5 categories (Likert scales, by default)
kj<-c(2,3,4,5)
# and these marginal distributions (set of cumulative probabilities)
marginal<-list(0.4,c(0.6,0.9),c(0.1,0.2,0.4),c(0.6,0.7,0.8,0.9))
corrcheck(marginal) # lower and upper bounds for Pearson's rho
```

```
corrcheck(marginal,Spearman=TRUE) # lower and upper bounds for Spearman's rho
# change the supports
support<-list(c(0,1),c(1,2,4),c(1,2,3,4),c(0,1,2,5,10))
corrcheck(marginal, support=support) # updated bounds
```

`ordcont` *computes the "intermediate" correlation matrix for the multivariate standard normal in order to achieve the "target" correlation matrix for the ordinal/discrete variables*

Description

The function computes the correlation matrix of the k-dimensional standard normal r.v. yielding the desired correlation matrix `Sigma` for the k-dimensional r.v. with desired marginal distributions `marginal`

Usage

```
ordcont(marginal,Sigma,support=list(),Spearman=FALSE,epsilon=1e-06,maxit=100)
```

Arguments

`marginal`	a list of k elements, where k is the number of variables. The i-th element of marginal is the vector of the cumulative probabilities defining the marginal distribution of the i-th component of the multivariate variable. If the i-th component has k_i categories, the i-th element of marginal will contain $k_i - 1$ probabilities (the k_i-th is obviously 1).
`Sigma`	the target correlation matrix of the ordinal/discrete variables
`support`	a list of k elements, where k is the number of variables. The i-th element of support contains the ordered values of the support of the i-th variable. By default, the support of the i-th variable is $1, 2, ..., k_i$
`Spearman`	if TRUE, the function finds Spearman's correlations (and it is not necessary to prvide `support`), if FALSE (default) Pearson's correlations
`epsilon`	the maximum tolerated error among target and actual correlations
`maxit`	the maximum number of iterations of the algorithm

Value

a list of four elements

`SigmaC`	the correlation matrix of the multivariate standard normal variable
`SigmaO`	the actual correlation matrix of the discretized variables (it should approximately coincide with the target correlation matrix `Sigma`)
`Sigma`	the target correlation matrix of the ordinal/discrete variables
`niter`	the number of iterations performed
`maxerr`	the actual maximum error (the absolute maximum deviation between actual and target correlations of the ordinal/discrete variables)

Note

The value of the maximum tolerated absolute error `epsilon` on the elements of the correlation matrix for ordinal r.v. can be set by the user: a value between 0.000001 and 0.01 seems to be an acceptable compromise assuring both the precision of the results and the convergence of the algorithm; moreover, a maximum number of iteration can be chosen (`maxit`), in order to avoid possible endless loops in case of non-convergence

Author(s)

Alessandro Barbiero, Pier Alda Ferrari

See Also

`contord`, `ordsample`, `corrcheck`

Examples

```
# consider a 4-dimensional ordinal variable
k<-4
# with different number of categories
kj<-c(2,3,4,5)
# and uniform marginal distributions
marginal<-list(0.5,c(1/3,2/3),c(1/4,2/4,3/4),c(1/5,2/5,3/5,4/5))
corrcheck(marginal)
# and the following correlation matrix
Sigma<-matrix(c(1,0.5,0.4,0.3,0.5,1,0.5,0.4,0.4,0.5,1,0.5,0.3,0.4,0.5,1),4,4,byrow=TRUE)
Sigma
# the correlation matrix of the standard 4-dimensional standard normal
# ensuring Sigma is
res<-ordcont(marginal, Sigma)
res[[1]]
# change some marginal distributions
marginal<-list(0.3,c(1/3,2/3),c(1/5,2/5,3/5),c(0.1,0.2,0.4,0.6))
corrcheck(marginal)
# and notice how the correlation matrix of the multivariate normal changes...
res<-ordcont(marginal, Sigma)
res[[1]]
# change Sigma, adding a negative correlation
Sigma[1,2]<--0.2
Sigma[2,1]<-Sigma[1,2]
Sigma
res<-ordcont(marginal, Sigma)
res[[1]]
```

`ordsample` *Drawing a sample of ordinal/discrete data*

Description

The function draws a sample from a multivariate ordinal/discrete variable with correlation matrix `Sigma` and pre-specified marginals `marginal`

Usage

```
ordsample(n, marginal, Sigma, support=list(), Spearman=FALSE, cormat="ordinal")
```

Arguments

`n`	the sample size
`marginal`	a list of k elements, where k is the number of variables. The i-th element of marginal is the vector of the cumulative probabilities defining the marginal distribution of the i-th component of the multivariate variable. If the i-th component has k_i categories, the i-th element of marginal will contain $k_i - 1$ probabilities (the k_i-th is obviously 1).
`Sigma`	the target correlation matrix of the ordinal/discrete variables
`support`	a list of k elements, where k is the number of variables. The i-th element of support contains the ordered values of the support of the i-th variable. By default, the support of the i-th variable is $1, 2, ..., k_i$
`Spearman`	if TRUE, the function finds Spearman's correlations (and it is not necessary to prvide `support`), if FALSE (default) Pearson's correlations
`cormat`	`ordinal` if the Sigma in input is the target correlation matrix of ordinal/discrete variables; `continuous` if the Sigma in input is the intermediate correlation matrix of the multivariate standard normal

Value

a $n \times k$ matrix of discrete/ordinal data drawn from the k-variate discrete/ordinal r.v. with the desired marginal distributions and correlation matrix

Author(s)

Alessandro Barbiero, Pier Alda Ferrari

See Also

`contord`, `ordcont`, `corrcheck`

Examples

```
# Example 1

# draw a sample from a bivariate ordinal variable
# with 4 of categories and asymmetrical marginal distributions
# and correlation coefficient 0.6 (to be checked)
k<-2
marginal<-list(c(0.1,0.3,0.6),c(0.4,0.7,0.9))
corrcheck(marginal) # check ok
Sigma<-matrix(c(1,0.6,0.6,1),2,2)
# sample size 1000
n<-1000
# generate a sample of size n
m<-ordsample(n, marginal, Sigma)
head(m)
# sample correlation matrix
cor(m) # compare it with Sigma
cumsum(table(m[,1]))/n
```

```
cumsum(table(m[,2]))/n # compare it with the two marginal distributions

# Example 1bis

# draw a sample from a bivariate ordinal variable
# with 4 of categories and asymmetrical marginal distributions
# and Spearman correlation coefficient 0.6 (to be checked)
k<-2
marginal<-list(c(0.1,0.3,0.6),c(0.4,0.7,0.9))
corrcheck(marginal, Spearman=TRUE) # check ok
Sigma<-matrix(c(1,0.6,0.6,1),2,2)
# sample size 1000
n<-1000
# generate a sample of size n
m<-ordsample(n, marginal, Sigma, Spearman=TRUE)
head(m)
# sample correlation matrix
cor(rank(m[,1]),rank(m[,2])) # compare it with Sigma
cumsum(table(m[,1]))/n
cumsum(table(m[,2]))/n # compare it with the two marginal distributions

# Example 2

# draw a sample from a 4-dimensional ordinal variable
# with different number of categories and uniform marginal distributions
# and different correlation coefficients
k<-4
marginal<-list(0.5,c(1/3,2/3),c(1/4,2/4,3/4),c(1/5,2/5,3/5,4/5))
corrcheck(marginal)
# select a feasible correlation matrix
Sigma<-matrix(c(1,0.5,0.4,0.3,0.5,1,0.5,0.4,0.4,0.5,1,0.5,0.3,0.4,0.5,1),4,4,byrow=TRUE)
Sigma
# sample size 100
n<-100
# generate a sample of size n
set.seed(1)
m<-ordsample(n, marginal, Sigma)
# sample correlation matrix
cor(m) # compare it with Sigma
cumsum(table(m[,4]))/n # compare it with the fourth marginal
head(m)
# or equivalently...
set.seed(1)
res<-ordcont(marginal, Sigma)
res[[1]] # the intermediate correlation matrix of the multivariate normal
m<-ordsample(n, marginal, res[[1]], cormat="continuous")
head(m)
```

Index

∗Topic **datagen**
    contord, 3
    ordcont, 5
    ordsample, 6
∗Topic **distribution**
    contord, 3
    corrcheck, 4
    ordcont, 5
    ordsample, 6
∗Topic **htest**
    contord, 3
    corrcheck, 4
    ordcont, 5
    ordsample, 6
∗Topic **models**
    contord, 3
    corrcheck, 4
    ordcont, 5
    ordsample, 6
∗Topic **package**
    GenOrd-package, 2

contord, *2*, 3, *4*, *6, 7*
corrcheck, *2, 3*, 4, *6, 7*

GenOrd-package, 2

ordcont, *2–4*, 5, *7*
ordsample, *2–4*, 6, *6*